

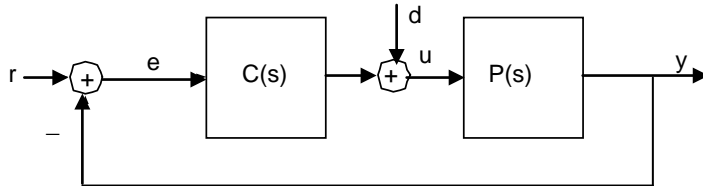
**EEE 304, Test 5**

**Name:** \_\_\_\_\_

Closed-book closed-notes, tables and calculators allowed, 30'

**Problem 1:**

For the feedback system shown below, compute the transfer functions from  $r$  to  $y$  ( $y/r$ ) and from  $d$  to  $u$  ( $u/d$ ).

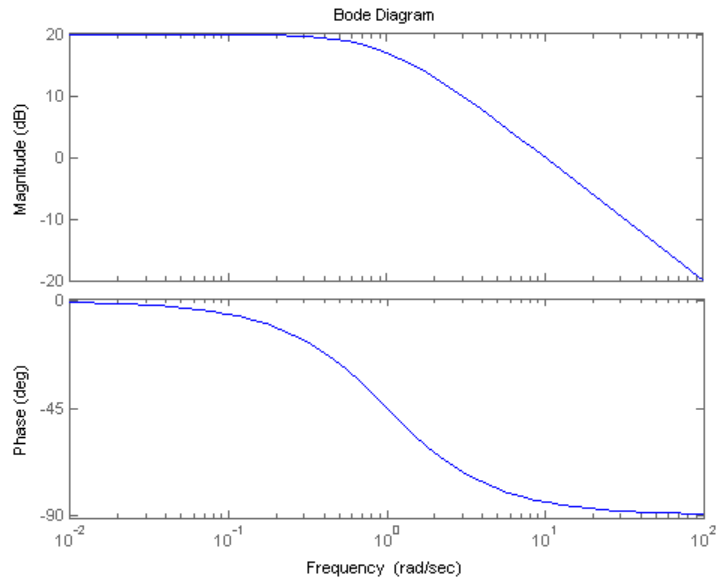


$$\frac{y}{r} = \frac{PC(s)}{1 + PC(s)}, \quad \frac{u}{d} = \frac{1}{1 + CP(s)}$$

**Problem 2:**

For the feedback system of Problem 1, suppose  $P(s) = 10/(s + 1)$  and  $C(s) = K(s + a)/s$ . Determine  $K, a$  so that the crossover frequency is 1rad/sec and the Phase Margin is at least  $60^\circ$ .

(You may use the given Bode plot to compute the necessary quantities graphically.)



At crossover, the phase condition is

$$\angle \frac{1}{j\omega_c} + \angle K + \angle(j\omega_c + a) + \angle \frac{10}{j\omega_c + 1} = -90^\circ + 0^\circ + \tan^{-1}(\omega_c / a) - \tan^{-1}(\omega_c / 1) \geq -180^\circ + 60^\circ$$

$$\Rightarrow \tan^{-1}(1/a) \geq 15^\circ \Rightarrow a = 3.7$$

Using this value we get the gain condition

$$\left| K \frac{j\omega_c + 3.7}{j\omega_c} \frac{10}{j\omega_c + 1} \right|_{\omega_c=1} = K \frac{10\sqrt{1+3.7^2}}{1\sqrt{1+1}} = 1 \Rightarrow K = 0.037$$

Thus controller transfer function is

$$C(s) = \frac{0.037 s + 0.137}{s}$$